

## Poster Pitch for #52

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September 25, 2025

[575] how one can physically realize:

partition function of topological gauge theories on quantum mechanics (SQM).

partition function of topological gauge theories on Ginzburg (LG) models.

theoretic Floer homologies (as 0-categories) and FS-type naturally allowed us to predict the existence of possibly higher

### Objectives

This poster is based on our work [3], and to:

1. Physically realize *novel* higher  $A_\infty$  gauge-theoretic Floer homologies furnishing physical proofs and generalizing conjectures by Bousseau-Doan-Reineke.
2. Systematically extend the scheme

### from Topological Gauge Theories with 16 Supercharges

$\times \mathbb{R}_t$  with real, simple, and compact gauge group  $G$

$$|F_{\mu\nu}^+|^2 + \left| F_{\mu\nu}^+ - \frac{1}{4}[B_{\mu\rho}, B_{\nu}{}^\rho] - \frac{1}{2}D_t B_{\mu\nu} \right|^2 + \dots,$$

$I_4 \times \mathbb{R}_t, \text{ad}(G))$  and a self-dual two-form

$$F^+ := (F + \star F)/2 \text{ and } [B_{\mu\rho}, B_{\nu}{}^\rho] \equiv g^{\rho\sigma}[B_{\mu\rho}, B_{\nu\sigma}].$$

### -type $A_\infty$ -2-categories



cast as 3d gauged LG models on  $\mathbb{R}^3$  in the irreducible holomorphic superpotential  $\mathcal{W}_D(\mathcal{X})$ , whose BPS deformed Fueter equations:

$$F^a - iF_{23} - jF_{31} - kF_{12} = g^{a\bar{b}} \left( \frac{e^{i\theta}}{2} \frac{\partial \mathcal{W}_D}{\partial \mathcal{X}^{\bar{b}}} \right)^* . \quad (1)$$

and LG SQM whose critical points now correspond to LG sheets the 1d LG SQM will physically realize an intersecting Floer homology thimbles  $(\mathfrak{P}^{***})$  representing the LG sheets, which, in turn, determine the physical Floer homology  $(F^{***})$  by the intersection

### 8d $\mathcal{N} = 1$ Spin(7) Theory

- Obtained via a “trivial” twist of 8d  $\mathcal{N} = 1$  SYM on 8d space and compact gauge group  $G$  [9]; it is topological in nature.
- The bosonic sector of its action is given by:

$$S_{\text{Spin}(7)} = \frac{1}{2e^2} \int_{\text{Spin}(7)} d^8x \text{Tr} \left( \frac{1}{2} F_{\mu\nu}^2 + \dots \right)$$

with an irreducible gauge connection  $A \in \Omega^1(\text{Spin}(7))$

$F^+ := (F + \star(\phi \wedge F))/2$  and  $\phi$  is the self-dual Spin(7)

### 4d gauged LG models and Cauchy-Riemann-Fuchs

#### $A_\infty$ -3-categories

- Gauge theories on  $M_D \times \mathbb{R}^1$  are first recast as 4d gauged LG models on the space of fields  $(\mathcal{X}, \mathcal{Y})$  on  $M_D$ , with holomorphic superpotential  $\mathcal{W}$ . If the equations are non-constant, gauged,  $\theta$ -deformed Cauchy-Riemann-Fuchs

$$(D_0 - \sum_{i=1}^3 I_i D_i) \mathcal{X}^a + I_1(F_{01} - F_{23}) + I_2(F_{02} + F_{13}) + I_3(F_{03} - F_{12}) = 0$$

- We further recast the theories as 1d LG SQM whose critical points correspond to threebranes in the equivalent 4d LG model. The 1d LG SQM

## Pros & Cons of Checking My Poster Out

### Pros

We will:

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2. Perform a "physical proof" of Mathematical conjectures.
3. Predict new Mathematical results from Physics.
4. Enjoy a nice diagram to summarise the results of 3 paper.

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### Cons

1. It's short: ~10 mins.

## Tomorrow's Presentation

### T18: Mathematical and Computational Physics

Friday, 26 Sept, 11:00am - Venue: Room 2; Chair: (TBD)

29 11:00am-11:15am	<b>Wenbo Wei, Nicholas Jia Le Chong, Choy Heng Lai, Ling Feng*</b> : Multiple Descents in Deep Learning as a Sequence of Order-Chaos Transitions
51★ 11:15am -11:30am	<b>Arif Er*, Meng-Chwan Tan</b> : Topological 5d $N=2$ Gauge Theories: Mirror Symmetry and Langlands Duality of A-infinity-categories of Floer Homologies
168 11:30am -11:45am	<b>Po-Yen Lai*</b> : Explaining the Bias Between Reanalysis Data and Observations During Heat Waves in East and Southeast Asian Cities: The Role of Urbanization and Urban Entropy